

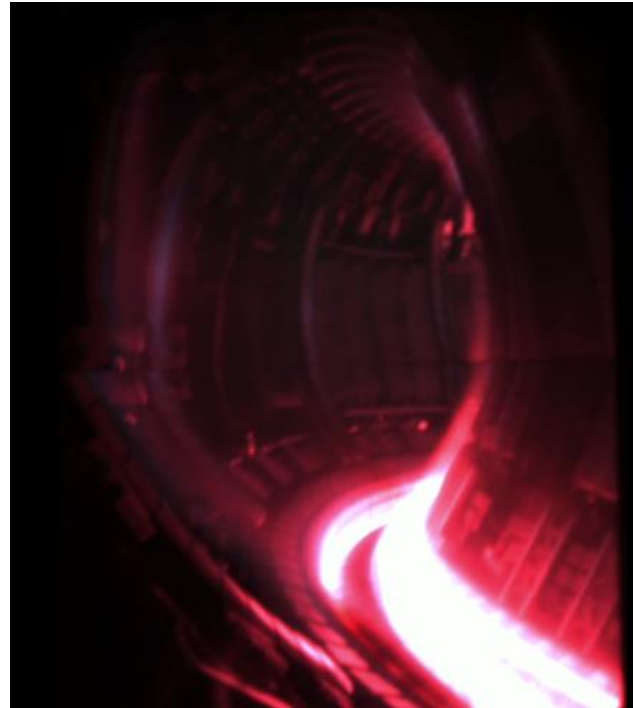
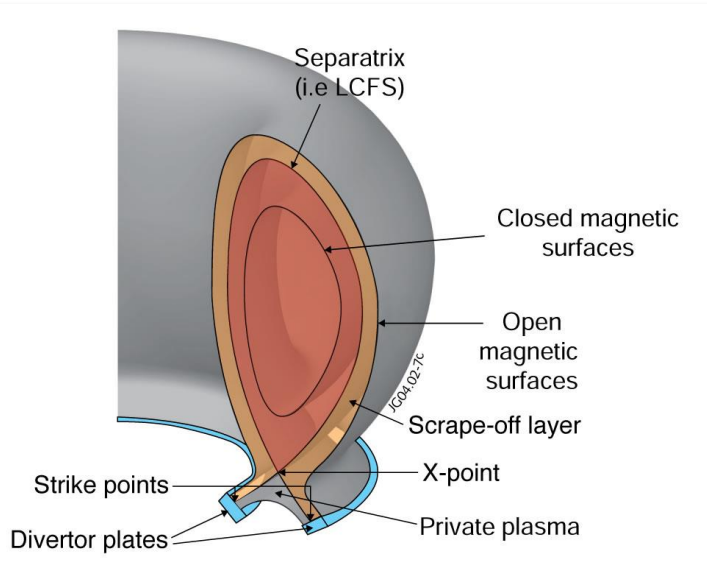
NESO-PARTICLES: A PERFORMANCE PORTABLE LIBRARY FOR FULL COUPLING OF PARTICLES TO FINITE ELEMENT FRAMEWORKS

Will Saunders, James Cook, UKAEA

ExCALIBUR Workshop 2023

ExCALIBUR NEPTUNE

- Modelling the plasma **edge/exhaust**.
- A long-established exascale grand-challenge **multi-physics, multi-scale** problem.
- **Complexity**: turbulence, many species, atomic physics, etc.
- Kinetic effects: out-of-thermal equilibrium matter (few collisions), **requires coupled fluid and particles**.



ITER Magnet Coils

Core Components

NESO

Particle Interface
Mesh coupling
Project
Evaluate

Solvers

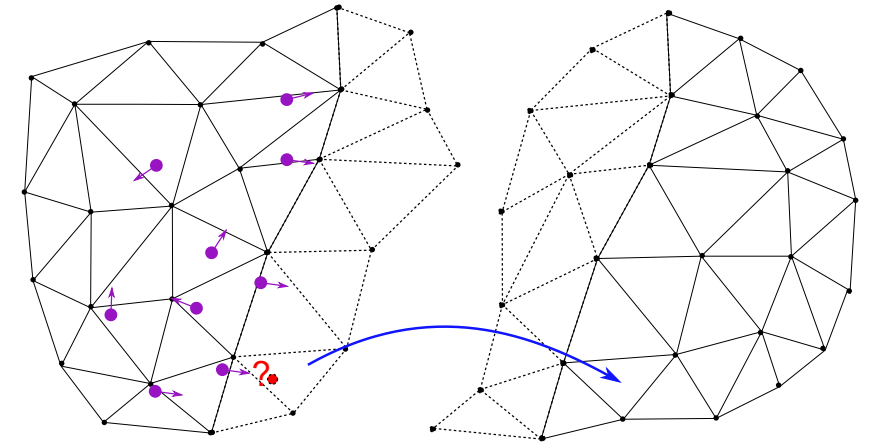
Nektar++

NESO-Particles

NESO-Spack

NESO-Particles: Core Components

- SYCL Particle framework
- Unstructured meshes
- **Particle data communication**
 1. Highly directional plasma flow (along field lines)
 2. Fast neutral flow (typically global and omnidirectional)
 3. Unstructured high-order mesh
- **Particle Based Operations/Data structures**
 1. Particle properties – position, velocity, charge, id...
 2. Loops over particles
 3. Degrees of Freedom (DOF) – Particle Loops
 4. Particle – Particle Loops

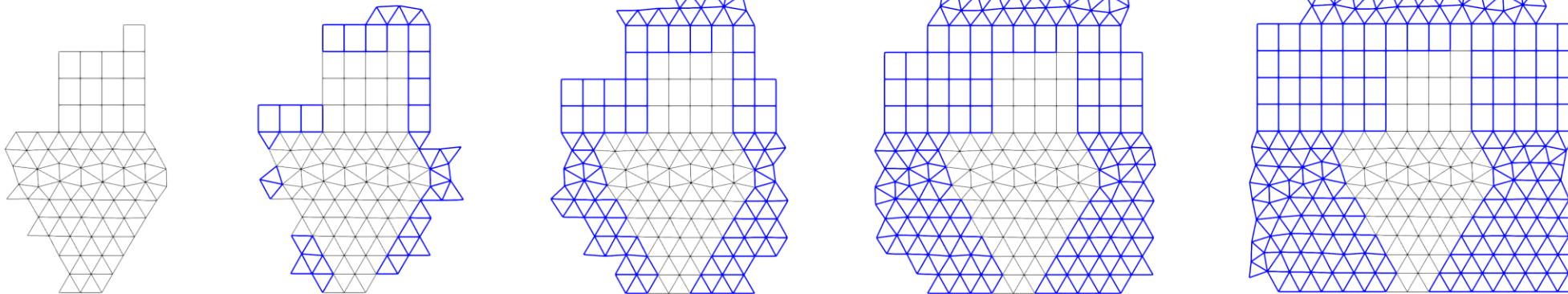
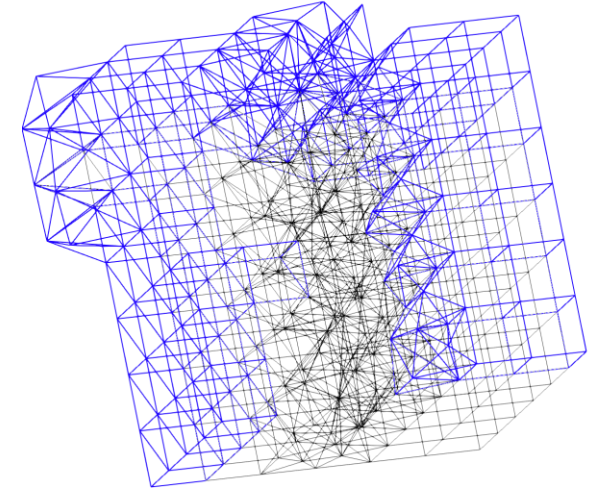


Combination of **halo regions** plus a **global move** method.

NESO-Particles: Halos

- Halos enable **local communication** patterns.
- Larger halo – more likely particle is communicated via local method.
- Can choose wider halo widths with faster particle movement.

3D halo building example.



Particle Data

ParticleGroup, ParticleDat

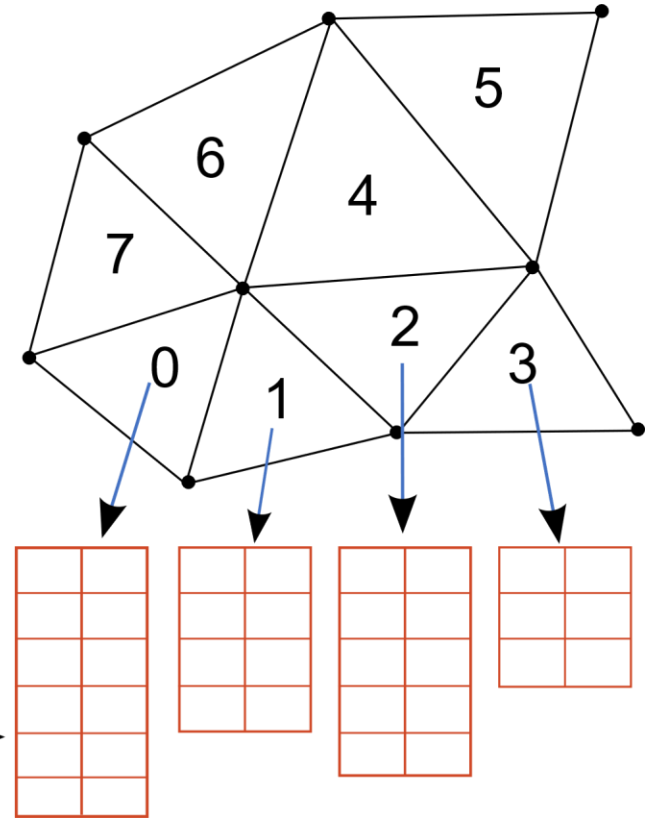
- Combines the: **mesh**, **compute device** and **particle data**.
- Implements particle bookkeeping – cells and MPI ranks.
- General particle properties, e.g. charge, mass, weight, velocity.

ParticleGroup

Domain: mesh

Compute device: SYCL Target

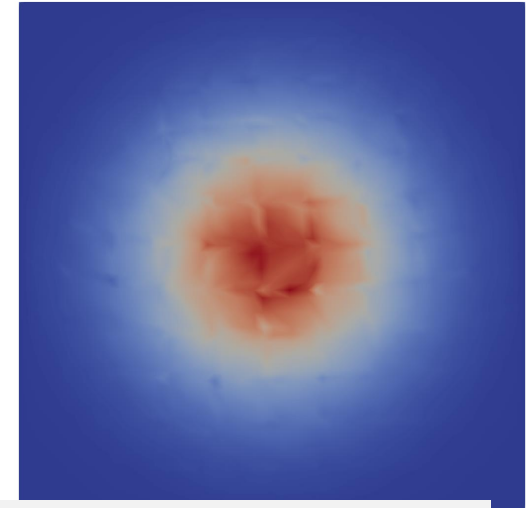
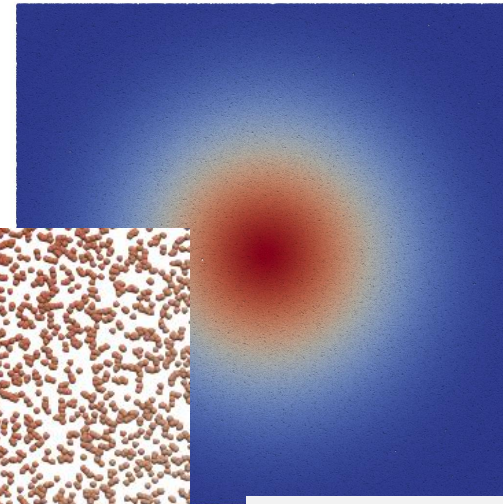
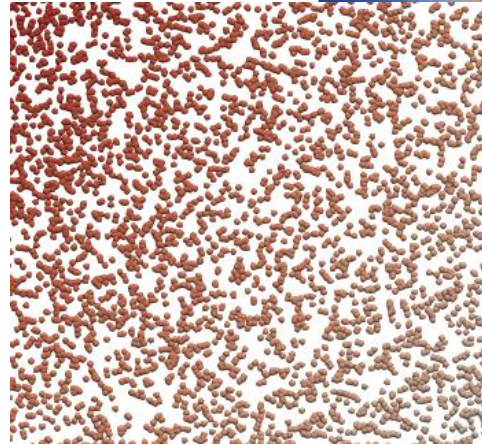
ParticleDat	PD	PD	PD
Name: "P"	"V"	"ID"	"Charge"
DType: REAL	REAL	INT	REAL
Ncomp: 2	3	1	1



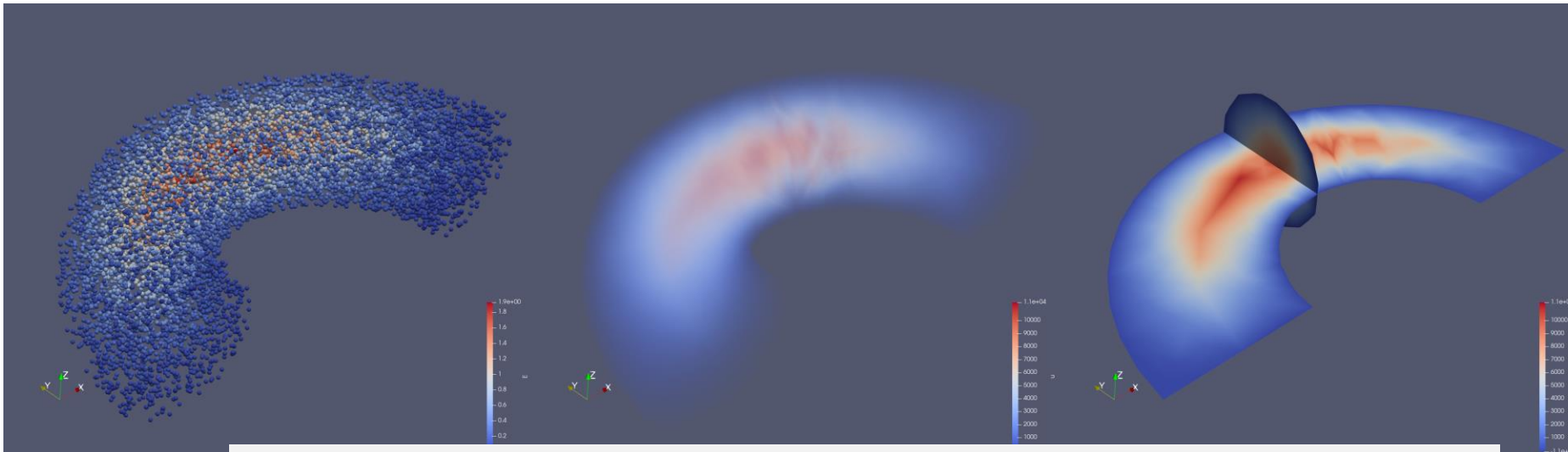
NESO

Coupling Finite Element Method and Particles

- Coupling from **particles to FEM** via L2 Galerkin projection.
- **FEM to particles** is point evaluation.
- Extends to **complex geometry**.



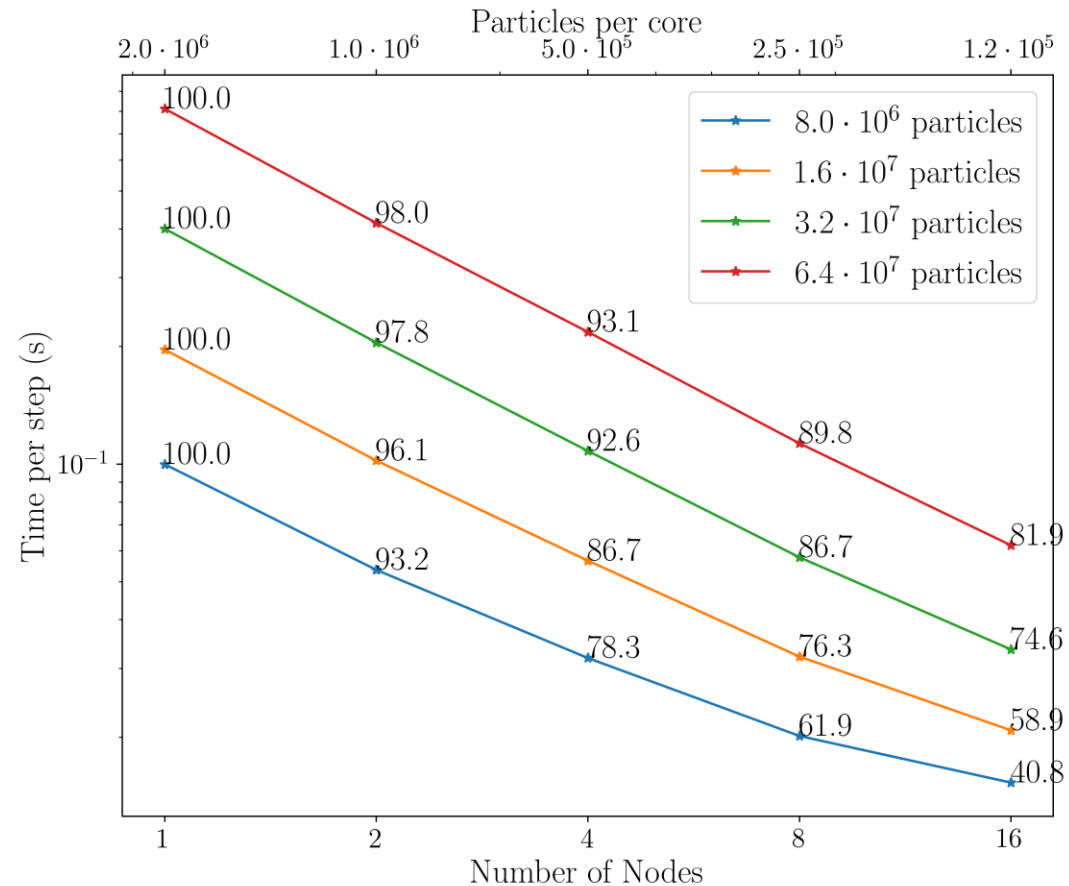
- **Uniformly** distributed positions
- **Gaussian** distributed weights



The End

*The support of the UK Meteorological Office
and Strategic Priorities Fund is acknowledged.*

Initial Profiling/Scaling

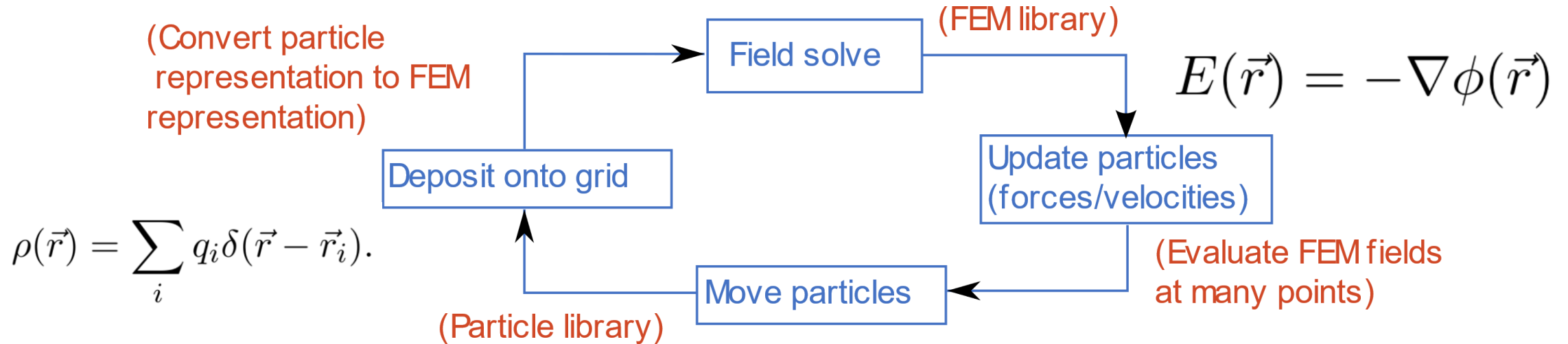


- Two-stream heavily biased towards particle work over finite element work.
- Strong scaling limit approximately 100k particles/core.

PIC Loop

Overview

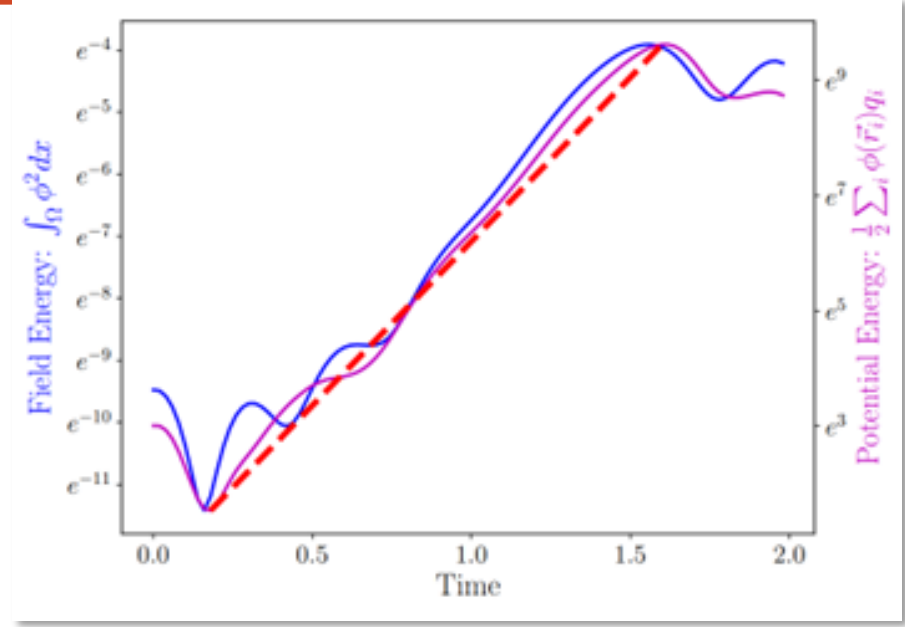
$$\Delta\phi(\vec{r}) = -\rho(\vec{r})$$



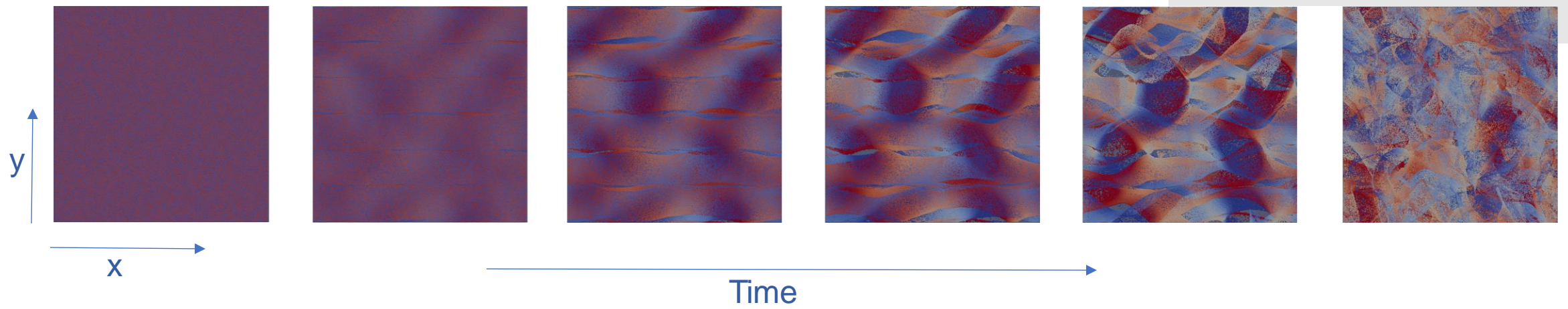
- Integration done with suitable integrator (Velocity-Verlet).
- **Synopsis** – More involved (and useful) schemes may combine steps.
- PIC schemes exist that **conserve quantities** of interest, e.g. **charge(mass)**, **energy** and momentum.
- Loop till convergence/end time.

Two Stream Instability

<p><u>NESO [1]</u></p>	<ul style="list-style-type: none"> • Test implementations integrating particle capabilities and FEM. • Can be built using Spack package manager. • 2D2V electrostatic particle-in-cell solver. • Nektar++ provides Poisson solve.
<p>Tests</p>	<ul style="list-style-type: none"> • Linear growth rates of unstable modes. • Energy conservation.



Instability growth rate vs theory

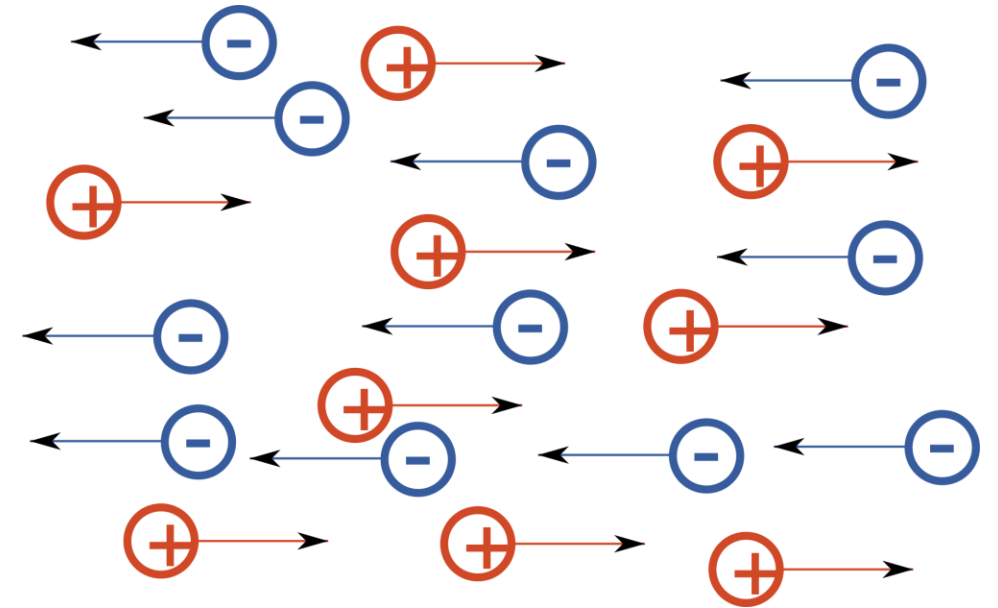


Time evolution (left to right) of 512k interacting particles. Colour is y-velocity.

Two Stream Instability

Motivational Example

- Periodic Boundary Conditions
- Overall charge neutral system
- Electrostatic interactions **through a mesh representation** (not point to point Coulomb interactions)
- Initial velocities are +1/-1 in x
- Unstable initial conditions



NESO Field Solve: Nektar++

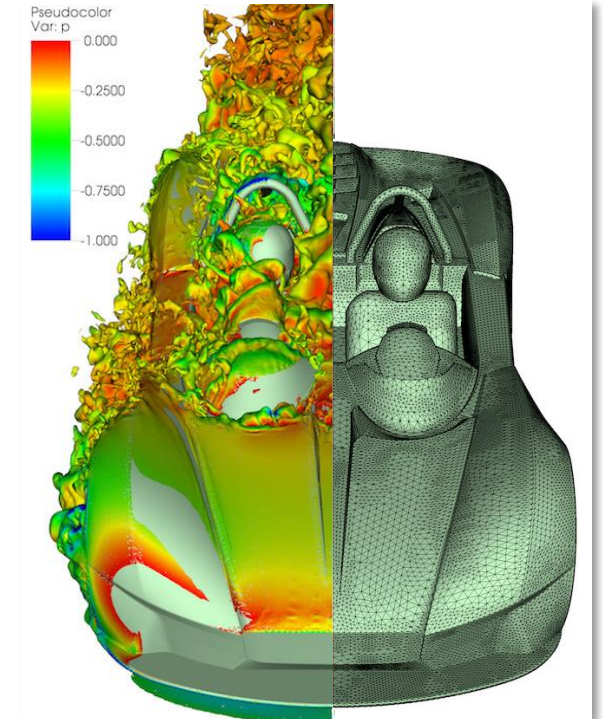
- Arbitrary convergence order p . (Error h^p (element size h)).
- Arithmetic intensity – increased number of operations on same data - counters HPC data movement bottleneck.
- Flow preferentially along field lines.
- Good support for complicated geometries, curved elements.

Structure	<ul style="list-style-type: none">• Set of libraries.• C++ code with MPI parallelism for CPUs.• Refactoring for performance portability / GPUs / C++17.
Provenance	<ul style="list-style-type: none">• Proven scaling to c.100k cores.• Well-tested code.• Established community of developers / users.
Benefit	<i>Good complex geometry support.</i>

1. <https://www.nektar.info>

D. Moxey (King's College London); C.D. Cantwell, S.J. Sherwin (Imperial College London)

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CFD simulation of Elemental RP1 track car.

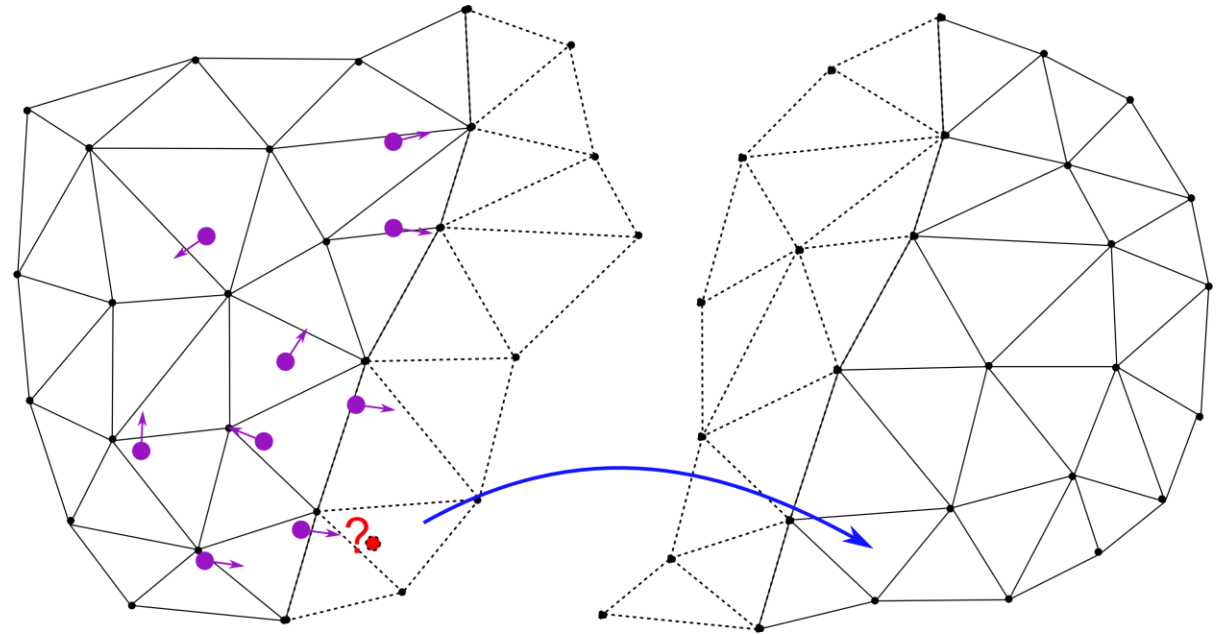
NESO-Particles

Global Particle Movement

- *Anywhere to Anywhere* particle movement supported (2D and 3D).
- Implemented with **halos + coarse grid**.
- **Tuneable** local communication via variable halo width.

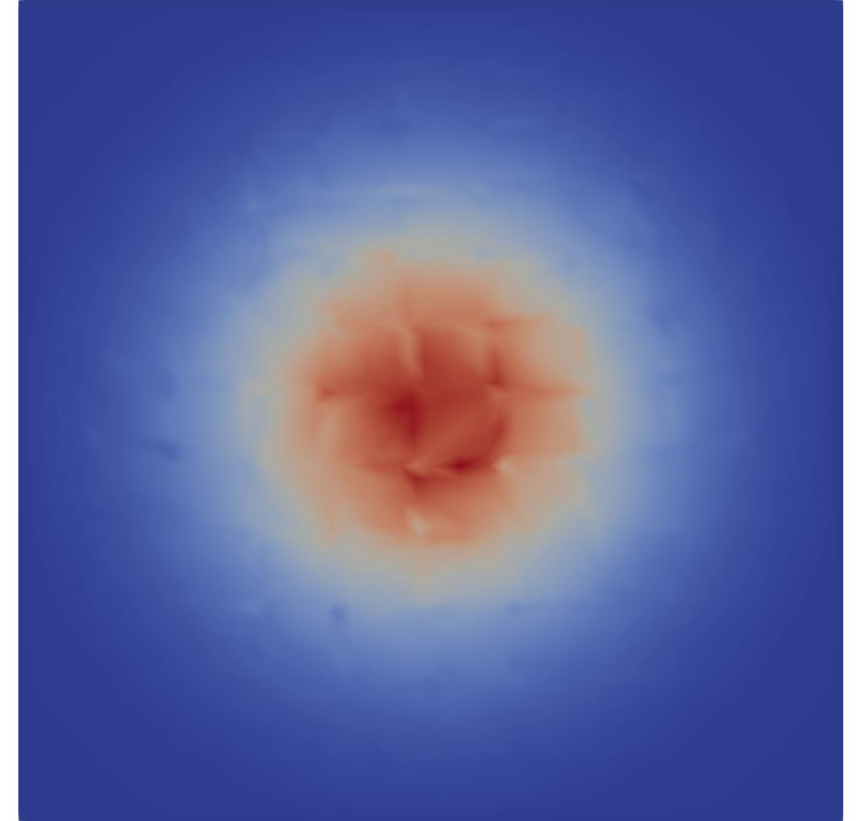
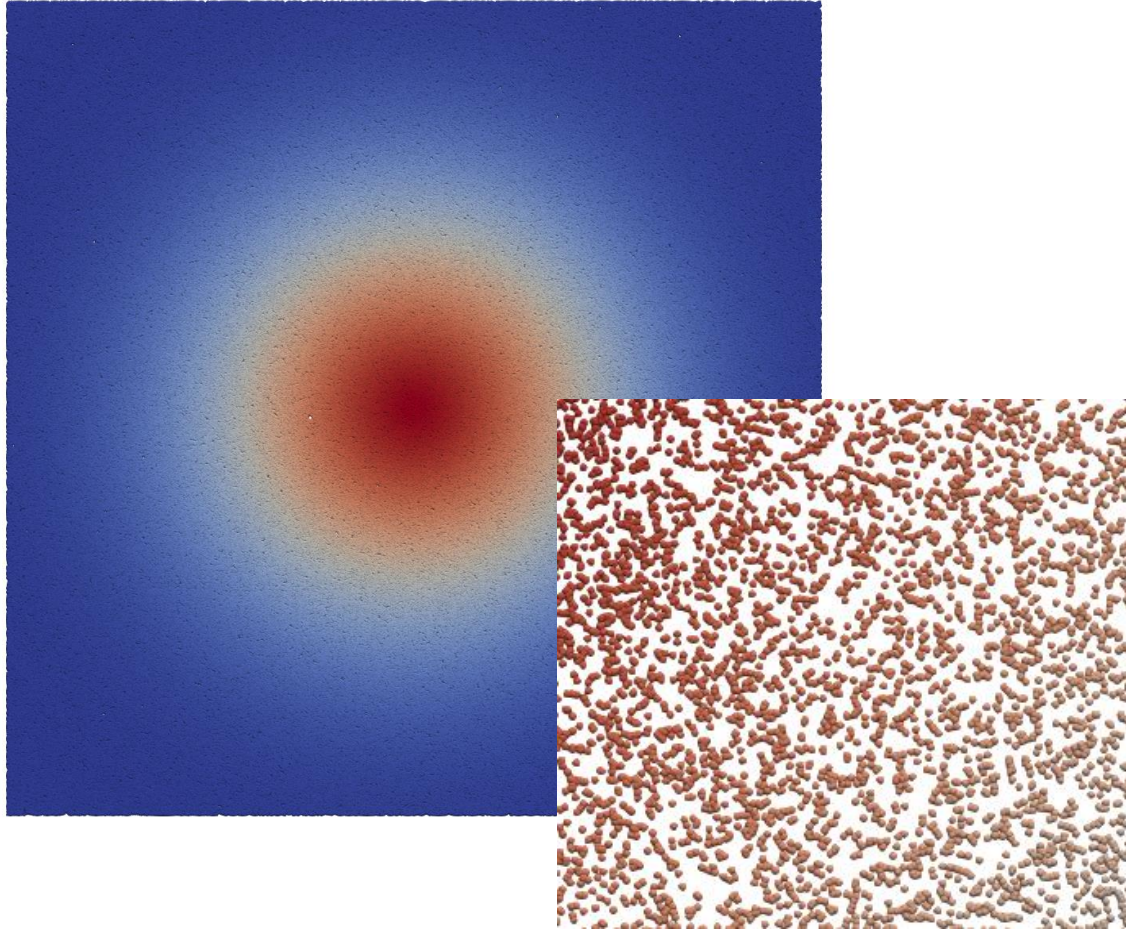
NESO:

- Bins particles into **2D** and **3D** elements.
- Caches reference positions (projection/evaluation).



Projection Example

500K particles. 10x10 Quadrilateral mesh



- **Uniformly** distributed positions
- **Gaussian** distributed weights

Projection

L2 Galerkin Projection

For particles indexed by i ,

$$\hat{\rho}(\vec{r}) = \sum_i q_i \delta(\vec{r} - \vec{r}_i)$$

- Particle representation

seek a function ρ such that

$$\rho(\vec{r}) = \sum_{j=1} \alpha_j \psi_j$$

- Finite element representation.

where

$$\langle \rho - \hat{\rho}, \psi_j \rangle = 0 \quad \forall j.$$

$$M\vec{\alpha} = \vec{\Psi},$$

Projection

L2 Galerkin Projection

$$M\vec{\alpha} = \vec{\Psi},$$

$$\begin{aligned}(\vec{\Psi})_j &= \langle \hat{\rho}, \psi_j \rangle \\ &= \sum_i q_i \int_{\Omega} \delta(\vec{r} - \vec{r}_i) \psi_j d\vec{x} \\ &= \sum_i q_i \psi_j(\vec{r}_i)\end{aligned}$$

- Dirac delta particle shape - No quadrature.

- Require evaluation of **each basis function** at **each particle location**.
- Implemented as SYCL kernels
- Static polymorphism (CRTP) for basis function types.
- CRTP as **virtual functions** are **not device callable**
- Given basis functions and DOFs – function evaluation is "easy".

Summary

Current status:

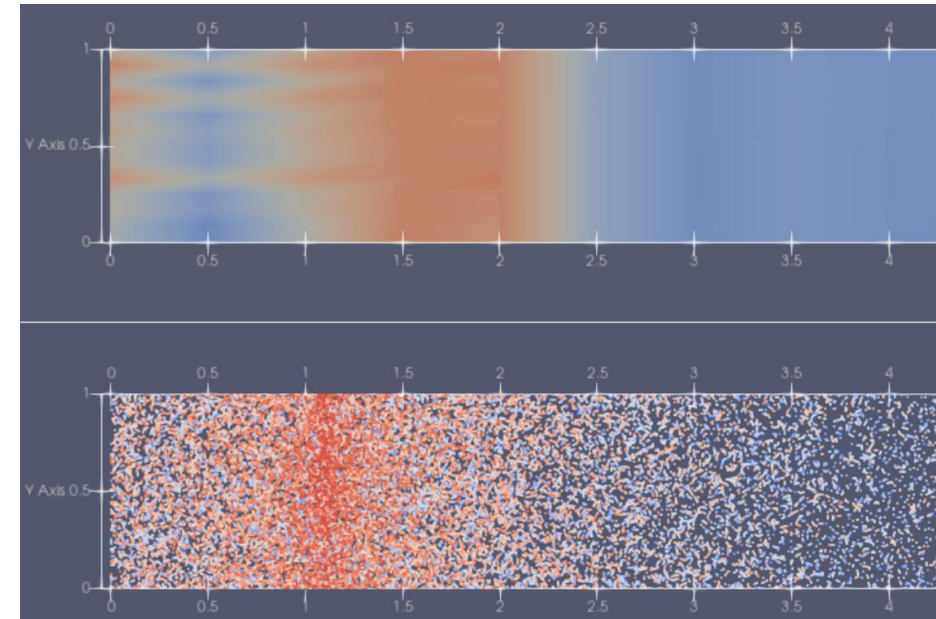
- Efficient particle coupling between finite elements and particles (**project/evaluate**).
- MPI+SYCL implementation (**CPU + GPU execution**).

In progress:

- Implementation of plasma turbulence models:
 1. Fluid approximation of plasma
 2. Kinetic Neutral species (particles)
 3. Plasma-Neutral coupling through project/evaluate
 4. Testing implementation using plasma turbulence problems

Continuous:

- Cycle of profile and improve implementations on CPU/GPU architectures.



ParticleLoop

Key:

- (standard) SYCL
- NESO-Particles API
- User Kernel

KERNEL_START/END are macros for CPU/GPU loop ordering

```
auto k_P = (*particle_group)[Sym<REAL>("POSITION")]->cell_dat.device_ptr();
auto k_V = (*particle_group)[Sym<REAL>("VELOCITY")]->cell_dat.device_ptr();

auto pl_iter_range = ...; auto pl_stride = ...; auto pl_npart_cell = ...;

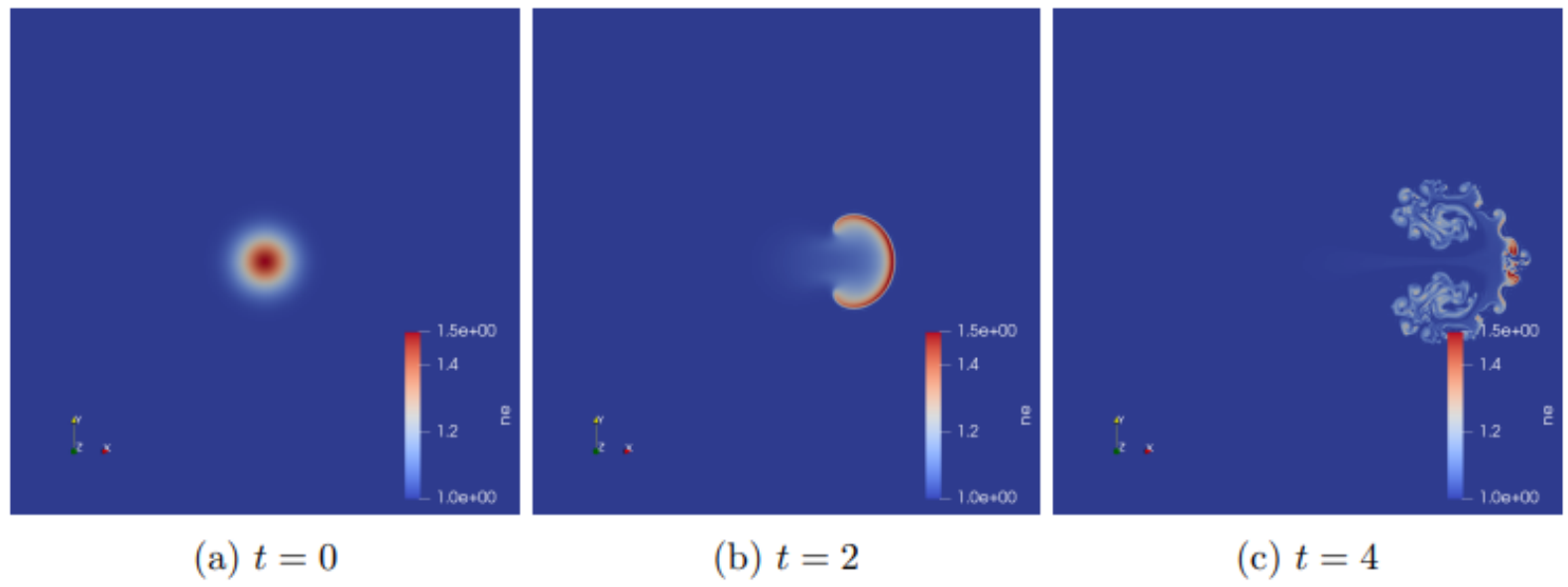
sycl_target->queue
    .submit([&](sycl::handler &cgh) {
        cgh.parallel_for<>(
            sycl::range<1>(pl_iter_range), [=](sycl::id<1> idx) {
                NESO_PARTICLES_KERNEL_START
                const INT cellx = NESO_PARTICLES_KERNEL_CELL;
                const INT layerx = NESO_PARTICLES_KERNEL_LAYER;

                k_P[cellx][0][layerx] += 0.001 * k_V[cellx][0][layerx];
                k_P[cellx][1][layerx] += 0.001 * k_V[cellx][1][layerx];

                NESO_PARTICLES_KERNEL_END
            });
    })
    .wait_and_throw();
```

Next steps: 2D3V plasma proxyapp

2D plasma turbulence with neutral particle source terms	<ul style="list-style-type: none">• Tight-coupled integration of the spectral / hp and particles.• Kinetic neutral species in plasma background.• Due by end Mar 2023.
Plasma turbulence in <i>Nektar++</i>	<i>Nektar++</i> [1] implementation of equations from existing <i>Hermes-3</i> code (finite difference) [2].
Neutral particles	Neutral particles do not feel confining magnetic field, but ionize as they interact with plasma – source terms in fluid equations (= coupling).



SYCL Experience

- **Thoughts:**
 1. CI – want to retain portability across SYCL implementations / hardware
 2. Developer/user environments – code needs to run on the pseudorandom environments in the wild.
 3. SYCL_EXTERNAL – optional in standard. **Nice to be able to write device functions.**
 4. 2020 spec significantly improves usability (64bit atomics, usm)
- **Works out-of-the-box:**
 1. Profiling, vtune/nvprof
 2. Composition with MPI

Code Generation

- **Kernel** and **loop structure** are captured (can perform higher level optimisations).
- Execution method is now tuneable and not the concern of the domain specialist (**separation of concerns**)
- Scope to alter how kernels perform more complex operations (**RNG, special functions**) on different hardware.
- Requires good abstractions:
 1. ParticleLoops, field deposition/evaluation are **first steps**.
 2. Neutral physics/molecular models are complex.

Code Generation – possible solution?

```
P = ParticleSymbol(..., "P"); V = ParticleSymbol(..., "V")
dt = Constant(0.001)
```

```
@kernel_inline
```

```
def dot_product_3d(a1, a2, a3, b1, b2, b3):
    return (a1 * b1) + (a2 * b2) + (a3 * b3)
```

```
@kernel_inline
```

```
def l2_squared_3d(a1, a2, a3):
    return dot_product_3d(a1, a2, a3, a1, a2, a3)
```

```
# Looping structure is captured
```

```
px = ParticleLoop()
```

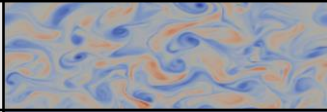
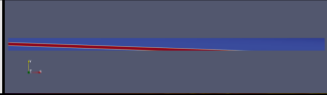

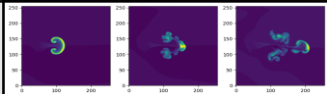
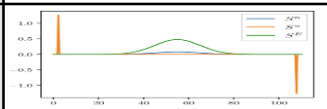
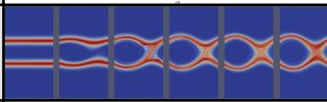
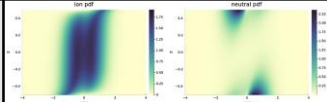
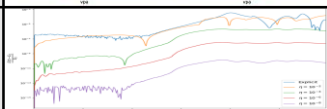
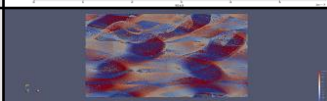
```
@kernel
```

```
def k_euler(P, V):
    for dx in range(2):
        P[px, dx] = P[px, dx] + dt * V[px, dx]
        ke = l2_squared_3d(V[px,0], V[px,1], V[px,2])
```

```
Loop(k_euler, P, V)
```

```
for (int dx = 0; dx < 2; dx+=1)
{
    P[neso_cellx][dx][neso_layerx] =
P[neso_cellx][dx][neso_layerx] +
0.001*V[neso_cellx][dx][neso_layerx];
}
auto a1_0 =
V[neso_cellx][0][neso_layerx];
auto a2_1 =
V[neso_cellx][1][neso_layerx];
auto a3_2 =
V[neso_cellx][2][neso_layerx];
auto a1_0_3 = a1_0;
auto a2_1_4 = a2_1;
auto a3_2_5 = a3_2;
auto b1_3_6 = a1_0;
auto b2_4_7 = a2_1;
auto b3_5_8 = a3_2;
auto ke = a1_0_3*b1_3_6 +
a2_1_4*b2_4_7 + a3_2_5*b3_5_8;
```

Proxyapps inventory

Proxyapp	Framework	Language	Comments	Sample output
nektar-driftwave	<i>Nektar++</i>	C++	2D Hasegawa-Wakatani equations	
nektar-diffusion	<i>Nektar++</i>	C++	strongly anisotropic diffusion	
vertical natural convection in spectral/ hp, 2D and 3D	<i>Nektar++</i>	C++	incompressible Navier-Stokes with buoyancy	
2D plasma turbulence equations in spectral/ hp	<i>Nektar++</i>	C++	<i>Hermes-3</i> equation system	
1D fluid solver with UQ and realistic boundary conditions	<i>Nektar++</i>	C++	1D model of scrape-off layer	
Vlasov-Poisson kinetic solver in spectral/ hp	<i>Nektar++</i>	C++	due Dec 2022	
moment-kinetics	new code (Univ. Oxford)	Julia	moment-kinetic gyro-averaged code	
minepoch	<i>EPOCH</i> (Univ. Warwick)	Fortran	used for testing particle implementations	
electrostatic PIC proxyapp	NESO-Particles	C++ / SYCL	due Dec 2022	
2D3V coupled fluids-neutral particles proxyapp	NESO-Particles	C++ / SYCL	due Mar 2023	coming soon

Community overview

UKAEA TEAM	Rob Akers, Wayne Arter, Matthew Barton, James Cook, John Omotani, Joseph Parker, Owen Parry, Will Saunders, Ed Threlfall.
UKRI GRANTS	<ul style="list-style-type: none">University of Exeter (WUQ, surrogate models): Peter Challenor, Tim Dodwell, Louise Kimpton.King's College London (Nektar++): Mashy Green, David Moxey.Imperial College London (Nektar++): Chris Cantwell, Bin Liu, Spencer Sherwin.University of Oxford: Michael Barnes, Patrick Farrell, Michael Hardman.STFC Hartree Centre: Vasil Alexandrov, Hussam al-Daas, Tyrone Rees, Emre Sahin, Andrew Sunderland, Sue Thorne.University College London (WUQ): Kevin Bronik, Peter Coveney, Matt Graham, Serge Guillas, Tuomas Koskela, Yiming Yang.University of Warwick (DSLs): Gihan Mudalige.University of York (plasma physics, support & coordination, DSLs): David Dickinson, Ed Higgins, Chris Ridgers, Steven Wright.
ALUMNI	<ul style="list-style-type: none">University of Oxford: Felix Parra-Diaz.University of Warwick (EPOCH): Ben McMillan, Tom Goffrey.University of York: Ben Dudson.
OUTPUT (INC. CODE)	<ul style="list-style-type: none">Proxyapps code (MIT licence): see repositories on https://github.com/ExCALIBUR-NEPTUNE (some, inc. NESO and NESO-Particles, are public).Large body of supporting documents and reports: https://github.com/ExCALIBUR-NEPTUNE/Documents (currently private).Developer website in development.

Participation welcomed!